## Acid - Base Equilibria 2

| Reading: | Ch 15 sections $8-12 \quad$ Homework: |
| :--- | :--- | | Chapter 15: 41, 57, 61*, 63, 65*, 67*, |
| :--- |
| $73^{*}, 85,87 *, 89,91$ |,

* = 'important' homework question


## Weak Acids



Review / Discussion: What is 'stronger' - HCl (aq) or vinegar (acetic acid)? What are the differences?

Because any weak acid and its respective dissociation products ( $\mathrm{H}^{+}$and conjugate base) are in equilibrium, 'equilibrium math' can be used to define K

Task: Determine an equilibrium expression (K) for the generic weak acid equilibrium:
$\mathrm{HA}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \Leftrightarrow \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq}) \quad+\mathrm{A}^{-}(\mathrm{aq})$
Weak Water Hydronium Conjugate
Acid ion

Base

Note: Since, in this case, K pertains to the dissociation of a weak acid only, it is called the acid dissociation constant and assigned a suitable subscript:

$$
\mathrm{K}_{\mathrm{a}}=\frac{\left[\mathrm{H}^{+}\right]\left[\mathrm{A}_{\text {weak }}^{-}\right]}{\left[\mathrm{HA}_{\text {weak }}\right]}
$$

Discussion: Will strong acids (like HCl ) have large or small values for $\mathrm{K}_{\mathrm{a}}$ ? Will weak acids (like acetic acid) have large or small values for $\mathrm{K}_{\mathrm{a}}$ ?

Task: Complete the following table:

| Acid | Type | Reaction with water | $\mathrm{K}_{\mathrm{a}}$ |
| :--- | :---: | :---: | :---: |
| HCl | strong | $\mathrm{HCl}(\mathrm{aq}) \rightarrow \mathrm{H}^{+}(\mathrm{aq})+\mathrm{Cl}^{-}(\mathrm{aq})$ | ${ }^{\prime} \infty^{\prime}$ |
| $\mathrm{HNO}_{3}$ |  |  |  |
| HF |  |  | $6.8 \times 10^{-4}$ |
| $\mathrm{HC}_{2} \mathrm{H}_{3} \mathrm{O}_{2}$ <br> $($ acetic) |  |  | $1.8 \times 10^{-4}$ |
| HCN |  |  | $4.9 \times 10^{-10}$ |

Discussion: Of all the weak acids listed above, which is the 'strongest', weakest? Why?

The Relationship Between $\mathrm{K}_{\mathrm{a}}$ and $\mathbf{p H}$


Overview: Since any weak acid is in equilibrium, a modified I.C.E. method can be used to determine either $\mathbf{p H}$ or $\mathbf{K}_{\mathrm{a}}$

Vanilla I.C.E., noted chemical philosopher

Worked Example: A sample of 0.10 M formic acid $\left(\mathrm{HCHO}_{2}\right)$ has a pH of 2.38. Determine $\mathrm{K}_{\mathrm{a}}$ for formic acid and the $\%$ to which formic acid is dissociated.

Plan:

1. Find $\left[\mathrm{H}^{+}\right]$
2. Set up and solve an I.C.E. table in order to find the equilibrium concentrations of $\mathrm{HA}, \mathrm{H}^{+}, \mathrm{A}^{-}$. 'Insert and evaluate' to find $\mathrm{K}_{\mathrm{a}}$

## 3. Find $\%$ dissociation

Using $\mathrm{K}_{\mathrm{a}}$ to find pH (the 'reverse' problem)
Question: What is the pH of $0.2 \mathrm{M} \mathrm{HCN}(\mathrm{aq})\left(\mathrm{K}_{\mathrm{a}}=4.9 \times 10^{-10}\right)$
Plan:

## Execution:



## IMPORTANT: The weak acid approximation: when $K_{a} \leq 10^{-3}$ $[\mathrm{HA}]-\left[\mathrm{H}^{+}\right] \approx[\mathrm{HA}]$

This greatly simplifies the I.C.E. method, which is usually not undertaken unless the above is true (would otherwise require a quadratic equation to be solved)

Group work: Skip ahead to the end of this handout and work through the first two practice exam problems

## Weak Bases



Weak base problems are very similar to the I.C.E. weak acid examples, except that $\left[\mathrm{OH}^{-}\right]$and pOH (rather than $\left[\mathrm{H}^{+}\right]$and pH ) are found initially

## Generic Equilibrium:

| $\underset{\text { Weak }}{\mathrm{B}(\mathrm{aq})}$ |
| :--- |
| Weak <br> base |$+\underset{\text { Water }}{\mathrm{H}_{2} \mathrm{O}(\mathrm{l})} \Leftrightarrow \underset{$|  Conjugate  |
| :--- |
|  Acid  |$}{\mathrm{HB}(\mathrm{aq})}+$| $\mathrm{OH}^{-}(\mathrm{aq})$ |
| :--- |
| Hydroxide |
| ion |

For ammonia dissolved in water:
$\mathrm{NH}_{3}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightarrow \mathrm{NH}_{4}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$

Task: Determine K for the above ammonia equilibrium

Note: Since, in this case, K pertains to the dissociation of a weak base only, it is called the base dissociation constant and assigned a suitable subscript:

Task: Complete the following table:

| Base | Type | Reaction with water | $\mathrm{K}_{\mathrm{a}}$ |
| :---: | :---: | :---: | :---: |
| NaOH | strong | $\mathrm{NaOH}(\mathrm{aq}) \rightarrow \mathrm{Na}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$ | ${ }^{\prime} \infty^{\prime}$ |
| KOH |  |  |  |
| $\mathrm{NH}_{3}$ |  |  | $1.8 \times 10^{-5}$ |
| $\mathrm{HS}^{-}$ |  |  | $1.8 \times 10^{-7}$ |
| $\mathrm{CO}_{3}{ }^{2-}$ |  |  | $1.8 \times 10^{-4}$ |

Discussion: Of all the weak bases listed above, which is the 'strongest', weakest? Why?

Example: Find $\left[\mathrm{OH}^{-}\right]$and pH for $0.15 \mathrm{M} \mathrm{NH}_{3}$ solution $\left(\mathrm{K}_{\mathrm{b}}=1.8 \times 10^{-5}\right)$
Plan:


Recall that [ $\mathrm{OH}-]$ and pOH can be found initially, then pH can be determined via:

$$
\mathrm{pH}+\mathrm{pOH}=14
$$

## Execution:

Group Task: $\mathrm{An} \mathrm{NH}_{3}(\mathrm{aq})$ solution has a pH of 10.50 . What is $\left[\mathrm{NH}_{3}\right]$ in this solution?

The Relationship between $\mathrm{K}_{a}$ and $\mathrm{K}_{\mathrm{b}}$
Recall: All weak acids and bases are in equilibrium with their respective conjugates. Each will also have an equilibrium (K) expression, e.g.:
$\mathrm{NH}_{4}^{+}(\mathrm{aq}) \rightarrow \mathrm{H}^{+}(\mathrm{aq})+\mathrm{NH}_{3}(\mathrm{aq}) ; \mathrm{K}_{\mathrm{a}}=$
$\mathrm{NH}_{3}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightarrow \mathrm{NH}_{4}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq}) ; \mathrm{K}_{\mathrm{b}}=$

'Equilibrium constant math' can be applied to the above pair of equations.

Task: Add the above equations and find an expression for K in terms of $\mathrm{K}_{\mathrm{a}}$ and $\mathrm{K}_{\mathrm{b}}$. Do you notice something familiar?

## $\pi$ For any weak acid or weak base:

$$
K_{a} K_{b}=K_{w}=1 \times 10^{-14}=\left[\mathrm{H}^{+}\right]\left[\mathrm{OH}^{-}\right]
$$

Also, since $\mathrm{K}_{\mathrm{a}} \mathrm{K}_{\mathrm{b}}=\mathrm{K}_{\mathrm{w}}$ :

$$
\mathbf{p K} \mathbf{K}_{\mathrm{a}}+\mathbf{p} \mathbf{K}_{\mathbf{b}}=\mathbf{p} K_{\mathrm{w}}
$$

Quick Question: What is $\mathrm{K}_{\mathrm{a}}$ for $\mathrm{NH}_{3}(\mathrm{aq})$ ?

Group work: Skip ahead to the last page of this handout and work through the practice exam problem 'Weak Base'

## "What's the pH? "

Question 2 ( 25 points): Calculate the pH of each of the following solutions:

1. $0.015 \mathrm{M} \mathrm{HCl}(\mathrm{aq})$ (assume complete dissociation)
2. $0.015 \mathrm{M} \mathrm{H}_{2} \mathrm{SO}_{4}(\mathrm{aq})$ (assume complete dissociation)
3. $0.015 \mathrm{M} \mathrm{NaOH}(\mathrm{aq})$ (assume complete dissociation)
4. $0.015 \mathrm{M} \mathrm{HC}_{2} \mathrm{H}_{3} \mathrm{O}_{2}(\mathrm{aq}), \mathrm{K}_{\mathrm{a}}=1.8 \times 10^{-5}$

## "Weak Acid"

Question 3 ( 25 points): A 0.200 M solution of a weak acid HA (aq) is $9.4 \%$ ionized (dissociated) at equilibrium. Use this information to calculate $\left[\mathrm{H}^{+}\right],[\mathrm{HA}]$ and $\mathrm{K}_{\mathrm{a}}$ for HA .

## "Weak Base"

Codeine $\left(\mathrm{C}_{18} \mathrm{H}_{21} \mathrm{NO}_{3}\right)$ is a weak organic base. A $5.0 \times 10^{-3} \mathrm{M}$ solution of codeine has a pH of 9.95 .

Question 4a (20 points): Calculate $\mathrm{K}_{\mathrm{b}}$ for codeine.

Question 4b (5 points): Calculate $\mathrm{pK}_{\mathrm{a}}$ for codeine.

Appendix:

## A Weak Acid

When HF dissolves in water, only a fraction of the molecules ionize.


## A Weak Base

$\mathrm{NH}_{3}$


Acid Strength
Acid
Base

| Strong | $\begin{gathered} \mathrm{Cl}^{-} \\ \mathrm{HSO}_{4}^{-} \\ \mathrm{NO}_{3}^{-} \end{gathered}$ | Neutral |
| :---: | :---: | :---: |
| $\mathrm{H}_{3} \mathrm{O}^{+}$ | $\mathrm{H}_{2} \mathrm{O}$ | Weak |
| $\mathrm{HSO}_{4}{ }^{-}$ | $\mathrm{SO}_{4}{ }^{2-}$ |  |
| $\mathrm{H}_{2} \mathrm{SO}_{3}$ | $\mathrm{HSO}_{3}{ }^{-}$ |  |
| $\mathrm{H}_{3} \mathrm{PO}_{4}$ | $\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}$ |  |
| HF | $\mathrm{F}^{-}$ |  |
| $\mathrm{HC}_{2} \mathrm{H}_{3} \mathrm{O}_{2}$ | $\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2}{ }^{-}$ |  |
| $\mathrm{H}_{2} \mathrm{CO}_{3}$ | $\mathrm{HCO}_{3}{ }^{-}$ |  |
| Weak $\mathrm{H}_{2} \mathrm{~S}$ | $\mathrm{HS}^{-}$ |  |
| $\mathrm{HSO}_{3}{ }^{-}$ | $\mathrm{SO}_{3}{ }^{2-}$ |  |
| $\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}$ | $\mathrm{HPO}_{4}{ }^{2-}$ |  |
| HCN | $\mathrm{CN}^{-}$ |  |
| $\mathrm{NH}_{4}^{+}$ | $\mathrm{NH}_{3}$ |  |
| $\mathrm{HCO}_{3}{ }^{-}$ | $\mathrm{CO}_{3}{ }^{2-}$ |  |
| $\mathrm{HPO}_{4}{ }^{2-}$ | $\mathrm{PO}_{4}{ }^{3-}$ |  |
| $\mathrm{H}_{2} \mathrm{O}$ | $\mathrm{OH}^{-}$ | Strong |
| Negligible | $\mathrm{S}^{2-}$ |  |
|  | $\mathrm{O}^{2-}$ |  |

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| Acid | Formula | Structural Formula | Ionization Reaction | $K_{\text {a }}$ |
| :---: | :---: | :---: | :---: | :---: |
| Chlorous acid | $\mathrm{HClO}_{2}$ | $\mathrm{H}-\mathrm{O}-\mathrm{Cl}=\mathrm{O}$ | $\begin{aligned} & \mathrm{HClO}_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \\ & \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{ClO}_{2}^{-}{ }^{-}(a q) \end{aligned}$ | $1.1 \times 10^{-2}$ |
| Nitrous acid | $\mathrm{HNO}_{2}$ | $\mathrm{H}-\mathrm{O}-\mathrm{N}=\mathrm{O}$ | $\begin{aligned} & \mathrm{HNO}_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \\ & \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{NO}_{2}^{-} \end{aligned}$ | $4.6 \times 10^{-4}$ |
| Hydrofluoric acid | HF | H-F | $\begin{aligned} & \mathrm{HF}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \\ & \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{F}^{-}(a q) \end{aligned}$ | $3.5 \times 10^{-4}$ |
| Formic acid | $\mathrm{HCHO}_{2}$ | $\begin{gathered} \\ \mathrm{H}-\mathrm{O}-\mathrm{C}-\mathrm{H} \end{gathered}$ | $\begin{array}{r} \mathrm{HCHO}_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \\ \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{CHO}_{2}{ }^{-}(a q) \end{array}$ | $1.8 \times 10^{-4}$ |
| Benzoic acid | $\mathrm{HC}_{7} \mathrm{H}_{5} \mathrm{O}_{2}$ |  | $\begin{array}{r} \mathrm{HC}_{7} \mathrm{H}_{5} \mathrm{O}_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \\ \mathrm{H}_{3} \mathrm{O}^{+}(a q) \end{array}+\mathrm{C}_{7} \mathrm{H}_{5} \mathrm{O}_{2}^{-}{ }^{-}(a q)$ | $6.5 \times 10^{-5}$ |
| Acetic acid | $\mathrm{HC}_{2} \mathrm{H}_{3} \mathrm{O}_{2}$ |  | $\begin{aligned} & \mathrm{HC}_{2} \mathrm{H}_{3} \mathrm{O}_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \\ & \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2}^{-}-(a q) \end{aligned}$ | $1.8 \times 10^{-5}$ |
| Hypochlorous acid | HClO | $\mathrm{H}-\mathrm{O}-\mathrm{Cl}$ | $\begin{aligned} & \mathrm{HClO}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \text { - } \\ & \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{ClO}^{-}(a q) \end{aligned}$ | $2.9 \times 10^{-8}$ |
| Hydrocyanic acid | HCN | $\mathrm{H}-\mathrm{C} \equiv \mathrm{N}$ | $\begin{aligned} & \mathrm{HCN}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \\ & \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{CN}^{-}(a q) \end{aligned}$ | $4.9 \times 10^{-10}$ |
| Phenol | $\mathrm{HC}_{6} \mathrm{H}_{5} \mathrm{O}$ |  | $\begin{array}{r} \mathrm{HC}_{6} \mathrm{H}_{5} \mathrm{O}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \\ \mathrm{H}_{3} \mathrm{O}^{+}(a q)+\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{O}^{-}(a q) \end{array}$ | $1.3 \times 10^{-10}$ |


| TABLE 15.10 Common Polyprotic Acids and lonization Constants |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Name (Formula) | Structure | $K_{\mathrm{a}_{1}}$ | $K_{\text {a }}$ | $K_{\text {a }}$ |
| Sulfuric Acid $\left(\mathrm{H}_{2} \mathrm{SO}_{4}\right)$ |  | Strong | $1.2 \times 10^{-2}$ |  |
| Oxalic Acid ( $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$ ) |  | $6.0 \times 10^{-2}$ | $6.1 \times 10^{-5}$ |  |
| Sulfurous Acid ( $\left.\mathrm{H}_{2} \mathrm{SO}_{3}\right)$ |  | $1.6 \times 10^{-2}$ | $6.4 \times 10^{-8}$ |  |
| Phosphoric Acid ( $\mathrm{H}_{3} \mathrm{PO}_{4}$ ) |  | $7.5 \times 10^{-3}$ | $6.2 \times 10^{-8}$ | $4.2 \times 10^{-13}$ |
| Citric Acid ( $\mathrm{H}_{3} \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{O}_{3}$ ) |  | $7.4 \times 10^{-4}$ | $1.7 \times 10^{-5}$ | $4.0 \times 10^{-7}$ |
| Ascorbic Acid ( $\mathrm{H}_{2} \mathrm{C}_{6} \mathrm{H}_{6} \mathrm{O}_{6}$ ) |  | $8.0 \times 10^{-5}$ | $1.6 \times 10^{-12}$ |  |
| Carbonic Acid ( $\left.\mathrm{H}_{2} \mathrm{CO}_{3}\right)$ |  | $4.3 \times 10^{-7}$ | $5.6 \times 10^{-11}$ |  |

## TABLE 15.8 Some Common Weak Bases

| Weak Base | Ionization Reaction | $\mathrm{K}_{\mathrm{b}}$ |
| :--- | :--- | :--- |
| Carbonate ion $\left(\mathrm{CO}_{3}{ }^{2-}\right)^{*}$ | $\mathrm{CO}_{3}{ }^{2-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{HCO}_{3}{ }^{-}(a q)+\mathrm{OH}^{-}(a q)$ | $1.8 \times 10^{-4}$ |
| Methylamine $\left(\mathrm{CH}_{3} \mathrm{NH}_{2}\right)$ | $\mathrm{CH}_{3} \mathrm{NH}_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{CH}_{3} \mathrm{NH}_{3}{ }^{+}(a q)+\mathrm{OH}^{-}(a q)$ | $4.4 \times 10^{-4}$ |
| Ethylamine $\left(\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{NH}_{2}\right)$ | $\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{NH}_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{C}_{2} \mathrm{H}_{5} \mathrm{NH}_{3}{ }^{+}(a q)+\mathrm{OH}^{-}(a q)$ | $5.6 \times 10^{-4}$ |
| Ammonia $\left(\mathrm{NH}_{3}\right)$ | $\mathrm{NH}_{3}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{NH}_{4}{ }^{+}(a q)+\mathrm{OH}^{-}(a q)$ | $1.76 \times 10^{-5}$ |
| Pyridine $\left(\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}\right)$ | $\mathrm{C}_{5} \mathrm{H}_{5} \mathrm{~N}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{C}_{5} \mathrm{H}_{5} \mathrm{NH}^{+}(a q)+0 \mathrm{H}^{-}(a q)$ | $1.7 \times 10^{-9}$ |
| Bicarbonate ion $\left(\mathrm{HCO}_{3}{ }^{-}\right)^{*}$ <br> (or hydrogen carbonate $)$ | $\mathrm{HCO}_{3}{ }^{-}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{H}_{2} \mathrm{CO}_{3}(a q)+\mathrm{OH}^{-}(a q)$ | $1.7 \times 10^{-9}$ |
| Aniline $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{2}\right)$ | $\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{2}(a q)+\mathrm{H}_{2} \mathrm{O}(l) \rightleftharpoons \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{NH}_{3}{ }^{+}(a q)+\mathrm{OH}^{-}(a q)$ | $3.9 \times 10^{-10}$ |

[^0]
[^0]:    *The carbonate and bicarbonate ions must occur with a positively charged ion such as $\mathrm{Na}^{+}$that serves to balance the charge but does not have any part in the ionization reaction. For example, it is the bicarbonate ion that makes sodium bicarbonate $\left(\mathrm{NaHCO}_{3}\right)$ basic. We look more closely at ionic bases in Section 15.8.

